

Lecture 6 24 Sept 07

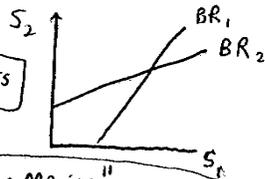
Last time: Investor Game

Lessons: communication can help in a coordination game
 - scope for leadership

NE = self-enforcing agreement

Not prisoners dilemma

Strategic Complements



	l	r
l	1, 1	0, 0
r	0, 0	1, 1

"Going to the Movies"

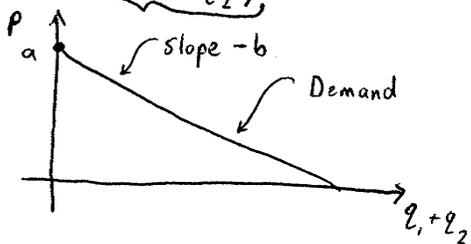
		2		
		BU	GS	SW
Bourne Ultimatum		2, 1	0, 0	0, -1
Good Shepherd		0, 0	1, 2	0, -1
Snow White		-1, 0	-1, 0	-2, -2

Nash Eq. = $\begin{cases} (BU, BU) \\ (GS, GS) \end{cases}$

BATTLE OF THE SEXES

"Cournot Duopoly" (ch. 6 of Dutta textbook)

- players 2 firms
- strategies quantities they produce of identical products q_1, q_2
- cost of production: cq constant marginal costs
- prices $p = a - b(q_1 + q_2)$



- payoffs: firms aim to maximize profit

$$u_i(q_1, q_2) = [p] q_i - c q_i$$

profits revenues cost

<< plug in price equation into profit equation >>

$$u_i(q_1, q_2) = a q_i - b q_i^2 - b q_i q_2 - c q_i$$

differentiate wrt (with respect to) $q_1 \rightarrow$ set = 0

$$\left\langle \frac{du_i}{dq_1} = 0 \right\rangle$$

F.o.C.

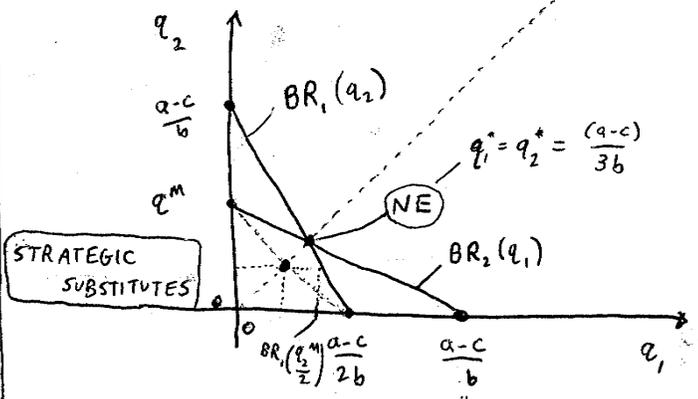
$$a - 2b q_1 - b q_2 - c = 0$$

S.o.C.

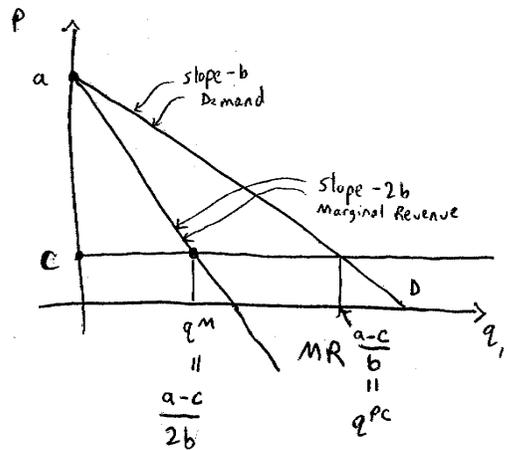
$$-2b < 0 \quad \checkmark$$

$$\hat{q}_1 = BR_1(q_2) = \frac{a-c}{2b} - \frac{q_2}{2}$$

$$\hat{q}_2 = BR_2(q_1) = \frac{a-c}{2b} - \frac{q_1}{2}$$



$$BR_1(0) = \frac{a-c}{2b}$$



<< when $BR_1 = 0$? >> $\frac{a-c}{2b} - \frac{q_2}{2} = 0 \Rightarrow q_2 = \frac{a-c}{b}$

<< Finding NE, intersection of $BR_1 = BR_2$ >>

$$q_1^* = q_2^*$$

$$q_1^* = \frac{a-c}{2b} - \frac{q_2^*}{2}$$

$$q_2^* = \frac{a-c}{2b} - \frac{q_1^*}{2}$$

$$q_1^* = \frac{a-c}{2b} - \frac{q_1^*}{2}$$

⋮

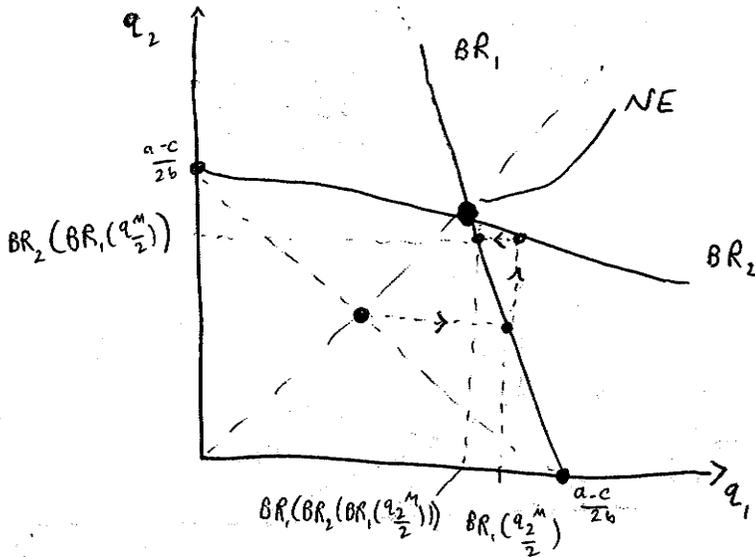
$$2q_1^* = \frac{a-c}{b} - q_2^*$$

$$3q_1^* = \frac{a-c}{b}$$

$$q_1^* = \frac{a-c}{3b} = q_2^*$$

COURNOT QUANTITY

STRATEGIC SUBSTITUTES



① << agreement breaks down from cheating, the graph heads back towards NE this won't always happen, but it does here >>

② << problem - may induce other entrants if you sustain profits eg. OPEC + competitive fringe Britain, Latin America >>

<< Compare to Monopoly / Competition: >>

Comp	Cournot		Monop	:	Q
$\frac{a-c}{b}$	$\frac{2}{3} \frac{a-c}{b}$	$\frac{1}{2} \frac{a-c}{b}$			
	prices			:	P
Comp	Cournot	monop			